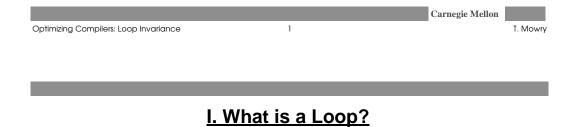
### Lecture 7

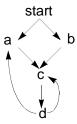
#### Loop Invariant Computation and Code Motion

- I Finding loops
- II Loop-invariant computation
- III Algorithm for code motion

Reference: Muchnick 13.2



- Goal:
  - Define a loop in graph-theoretic terms (control flow graph)
  - Not sensitive to input syntax, a uniform treatment for all loops: DO, while, goto's
- Not every cycle is a "loop" from the optimization perspective

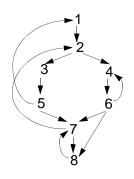


- Intuitive properties of a loop
  - · single entry point
  - edges must form at least a cycle



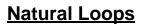
## **Formal Definitions**

- Dominators
  - Node *d* dominates node *n* in a graph (*d* dom *n*) if every path from the start node to *n* goes through *d*



- Dominators can be organized as a tree
  - a->b in the dominator tree iff a immediately dominates b

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#### • Definitions

- Single entry-point: *header* 
  - a header dominates all nodes in the loop
- A back edge is an arc whose head dominates its tail (tail -> head)
  - · a back edge must be a part of at least one loop
- The *natural loop of a back edge* is the smallest set of nodes that includes the head and tail of the back edge, and has no predecessors outside the set, except for the predecessors of the header.



## **Algorithm to Find Natural Loops**

- 1. Find the dominator relations in a flow graph
- 2. Identify the back edges
- 3. Find the natural loop associated with the back edge



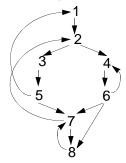
## **<u>1. Finding Dominators</u>**

#### • Definition

- Node *d* dominates node *n* in a graph (*d* dom *n*) if every path from the start node to *n* goes through *d*
- Formulated as MOP problem
  - node *d* lies on all possible paths reaching node  $n => d \operatorname{dom} n$ 
    - Direction:
    - Values:
    - Meet operator:
    - Top:
    - Bottom:
    - Boundary condition: start/entry node =
    - Initialization for internal nodes
    - Finite descending chain?
    - Transfer function:
- Speed:
- With reverse postorder, most flow graphs (reducible flow graphs) converge in 1 pass

## 2. Finding Back Edges

- Depth-first spanning tree
  - Edges traversed in a depth-first search of the flow graph form a depth-first spanning tree



#### • Categorizing edges in graph

- · Advancing edges: from ancestor to proper descendant
- Cross edges: from right to left
- Retreating edges: from descendant to ancestor (not necessarily proper)

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**Back Edges** 

#### Definition

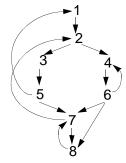
- Back edge: t->h, h dominates t
- Relationships between graph edges and back edges
- Algorithm
  - Perform a depth first search
  - For each retreating edge t->h, check if h is in t's dominator list
- Most programs (all structured code, and most GOTO programs) -- reducible flow graphs

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retreating edges = back edges

## **<u>3. Constructing Natural Loops</u>**

- The *natural loop of a back edge* is the smallest set of nodes that includes the head and tail of the back edge, and has no predecessors outside the set, except for the predecessors of the header.
- Algorithm
  - delete h from the flow graph
  - find those nodes that can reach t
     (those nodes plus h form the natural loop of t ->h)

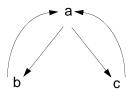


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Inner Loops

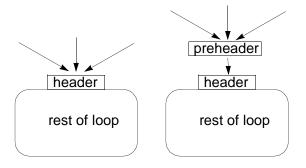
- · If two loops do not have the same header
  - · they are either disjoint, or
  - one is entirely contained (nested within) the other -- inner loop, one that contains no other loop.
- · If two loops share the same header
  - Hard to tell which is the inner loop
     Combine as one





# Preheader

- Optimizations often require code to be executed once before the loop
- Create a preheader basic block for every loop



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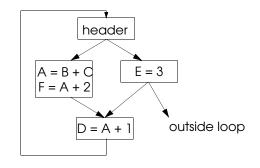
# Finding Loops: Summary

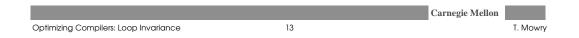
- Define loops in graph theoretic terms
- Definitions and algorithms for
  - Dominators
  - Back edges
  - Natural loops

### **II. Loop-Invariant Computation and Code Motion**

### • A loop-invariant computation:

- a computation whose value does not change as long as control stays within the loop
- Code motion:
  - to move a statement within a loop to the preheader of the loop





## <u>Algorithm</u>

#### • Observations

- Loop invariant
  - operands are defined outside loop or invariant themselves
- Code motion
  - not all loop invariant instructions can be moved to preheader
- Algorithm
  - Find invariant expressions
  - Conditions for code motion
  - Code transformation

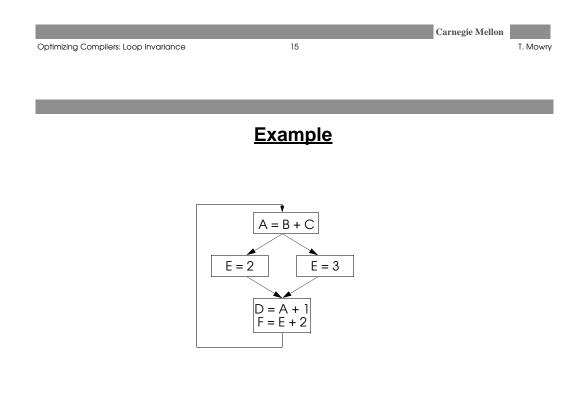
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# **Detecting Loop Invariant Computation**

- · Compute reaching definitions
- Mark INVARIANT if all the definitions of B and C that reach a statement A=B+C are outside the loop
  - constant B, C?
- Repeat: Mark INVARIANT if
  - · all reaching definitions of B are outside the loop, or
  - there is exactly one reaching definition for B, and it is from a loop-invariant statement inside the loop
  - similarly for C

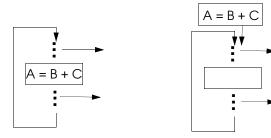
until no changes to set of loop-invariant statements occur.





## **III. Conditions for Code Motion**

- Correctness: Movement does not change semantics of program
- Performance: Code is not slowed down



- Basic idea: defines once and for all
  - control flow:
  - other definitions:
  - other uses:

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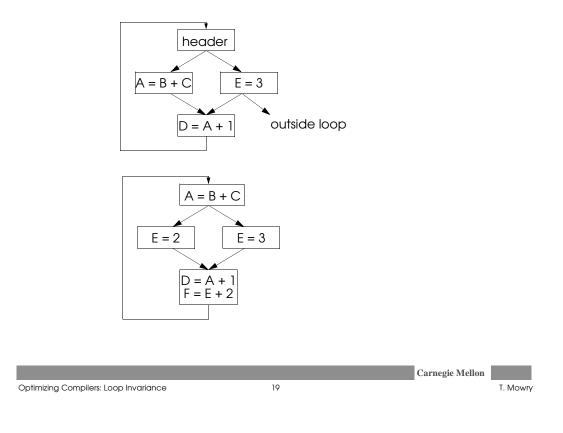
## Code Motion Algorithm

Given: a set of nodes in a loop

- Compute reaching definitions
- Compute loop invariant computation
- Compute dominators
- Find the exits of the loop, nodes with successor outside loop
- Candidate statement for code motion:
  - loop invariant
  - in blocks that dominate all the exits of the loop
  - assign to variable not assigned to elsewhere in the loop
  - in blocks that dominate all blocks in the loop that use the variable assigned
- Perform a depth-first search of the blocks
  - Move candidate to preheader if all the invariant operations it depends on have been moved



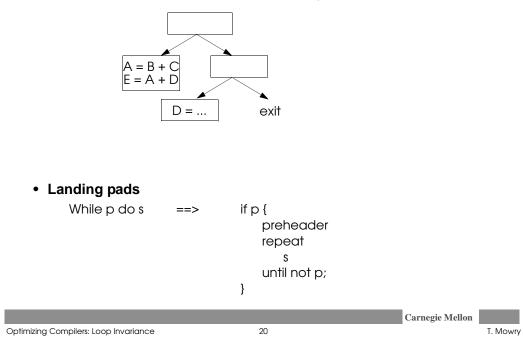
# **Examples**



## **More Aggressive Optimizations**

### • Gamble on: most loops get executed

· Can we relax constraint of dominating all exits?



# **Conclusions**

- Precise definition and algorithm for loop invariant computation
- Precise algorithm for code motion
- Use of reaching definitions and dominators in optimizations

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