

## Why cite?

- Citations reflect *the careful and thorough work you have put in* to locating and exploring your sources.
- Citations *help readers understand the context* of your argument, and locate your work within other conversations on your topic.
- Citations allow you to *acknowledge those authors who made possible particular aspects of your work*. Failure to provide adequate citations constitutes plagiarism.
- Citations, by delineating your intellectual debts, also *draw attention to the originality and legitimacy of your own ideas*.

<http://www.dartmouth.edu/~sources/about/what.html>

## When to cite?

- Cite sources for all verbatim quotations of two or more consecutive words.
- Cite sources from which you paraphrase or summarize facts or ideas.
- Cite sources for ideas or information that could be regarded as common knowledge but which you think your reader might still find unfamiliar.

<http://www.dartmouth.edu/~sources/about/what.html>

## What to cite?

**Primarily:** *refereed, archival* materials. (Archival materials are materials that are available in libraries or bookstores, have an ISBN number, etc.)

- Books
- Journal articles
- Refereed conference proceedings

**Avoid:**

- Websites, news stories, photocopied workshop handouts, personal communications.

### The original text:

The main image in *Othello* is that of animals in action, preying upon one another, mischievous, lascivious, cruel or suffering, and through these, the general sense of pain and unpleasantness is much increased and kept constantly before us.

More than half the animal images in the play are Iago's, and all these are contemptuous or repellent: a plague of flies, a quarrelsome dog, the recurrent image of bird-snaring, leading asses by the nose, a spider catching a fly, beating an offenceless dog, wild cats, wolves, goats and monkeys<sup>1</sup>.

1. Caroline F. E. Spurgeon, *Shakespeare's Imagery* (Cambridge: Cambridge UP, 1935) 335.

### Students paper:

The majority of the animal images in the play are Iago's, and all of these are contemptuous or repellent. He refers to a plague of flies, a quarrelsome dog, bird-snaring, leading asses by the nose, a spider catching a fly, beating an offenceless dog, wild cats, goats and monkeys. Through these images the general sense of pain and unpleasantness is increased and kept constantly before us.

<http://www.dartmouth.edu/~sources/about/w>

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<http://www.dartmouth.edu/~sources/about/w>

**Not OK:**

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<http://www.dartmouth.edu/~sources/about/w>

**Not OK:**

**Students paper:**

I believe that the main image in Shakespeare's tragedy, *Othello*, is that of animals. These creatures are constantly in action, preying upon one another, and they are depicted as mischievous, wanton, cruel or suffering. By Shakespeare's ingenious use of these animal images, the general sense of pain and unpleasantness that pervades the entire story is much increased and kept constantly before the reader.

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<http://www.dartmouth.edu/~sources/about/w>

**Not OK:**

**Students paper:**

In *Othello*, Shakespeare makes frequent use of animal imagery. The specific images he uses are generally distasteful and convey to the reader a constant impression of conflict and misery.

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The main image in *Othello* is that of animals in action, preying upon one another, mischievous, lascivious, cruel or suffering, and through these, the general sense of pain and unpleasantness is much increased and kept constantly before us.

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1. Caroline F. E. Spurgeon, *Shakespeare's Imagery* (Cambridge: Cambridge UP, 1935) 335.

<http://www.dartmouth.edu/~sources/about/w>

**OK:**

**Students paper:**

In the play, *Othello*, the character of Iago is associated with unpleasant animal imagery[1]...

1. Caroline F. E. Spurgeon, *Shakespeare's Imagery* (Cambridge: Cambridge UP, 1935) 335.

**The original text:**

The main image in *Othello* is that of animals in action, preying upon one another, mischievous, lascivious, cruel or suffering, and through these, the general sense of pain and unpleasantness is much increased and kept constantly before us.

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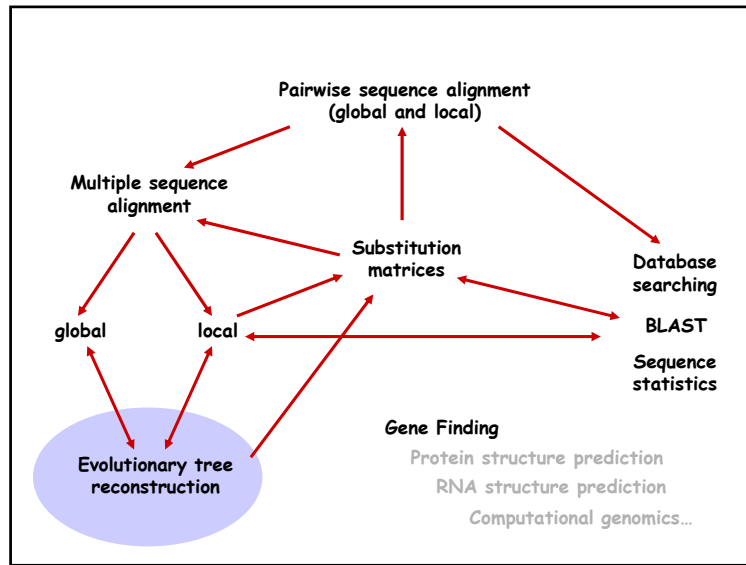
**OK:**

**Students paper:**

Caroline Spurgeon uses the words "contemptuous" and "repellent" in describing the animal imagery associated with Iago in *Othello* [1]. In my opinion, her choice of words indicates that...

1. Caroline F. E. Spurgeon, *Shakespeare's Imagery* (Cambridge: Cambridge UP, 1935) 335.

<http://www.dartmouth.edu/~sources/about/w>



### Selecting data for tree reconstruction

- For reconstructing recent events, use DNA sequences
- For reconstructing distant events, use amino acid sequences
- Select sequences that
  - Are present in all taxa
  - Contain a conserved region
  - Exhibit variation within that region
  - e.g., Ribosomal (16sRNA) genes were used to reconstruct the tree of life. These genes encode products use in all organisms from bacteria to mammals.
- Pitfalls: duplicated genes, horizontal gene transfer, mosaic genes.

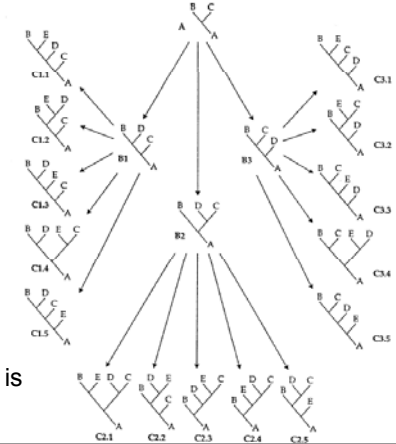


## The number of trees gets big fast

Number of leaves	Number of unrooted binary trees
3	1
4	3
5	15
6	105
10	2,027,025
20	$2.2 \times 10^{20}$
50	$2.8 \times 10^{74}$
500	$1 \times 10^{1074}$

## How do you find the optimal tree?

1. Exhaustive search (<12 taxa)



(Phylogeny reconstruction is NP-complete.)

## How do you find the optimal tree?

Method	Result	Time	Typical k
Exhaustive search	Optimal solution	$T(k)$	12

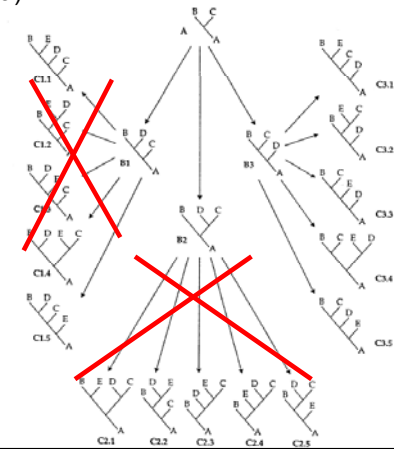
## How do you find the optimal tree?

2. Branch-and-bound (<18 taxa)

Score is non-decreasing as you add edges

```

L = {T3}, C = infinity
For i = 3 to k {
  For each tree, t, in L{
    If Score(t) > C, skip
    If Score(t) < C, C = Score(t).
    For every edge, e, in t {
      t' = t plus a new edge at e
      NewL = NewL U {t'}
    }
  }
  L = NewL
}
    
```



## How do you find the optimal tree?

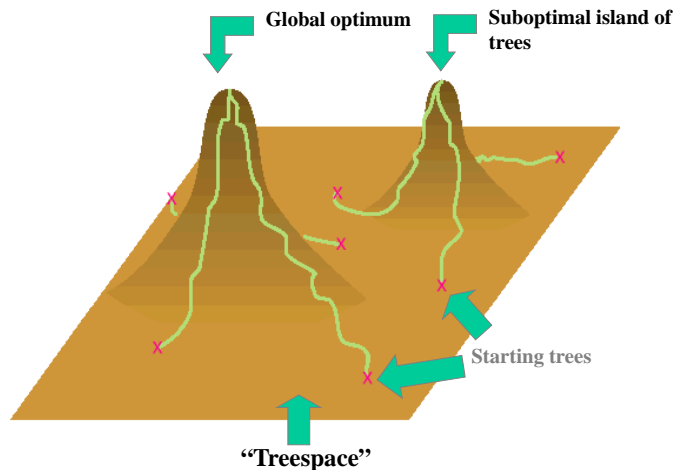
Method	Result	Time	Typical k
<b>Exhaustive search</b>	Optimal solution	$T(k)$	12
<b>Branch and bound</b>	Optimal solution	$\leq T(k)$	18

## How do you find a pretty good tree?

### 3. Heuristic search

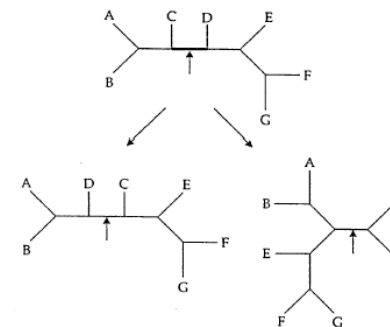
Search for optimal trees by finding good trees and then rearranging them in the hopes of finding an even better tree

## Heuristic search



## Branch swapping

### Nearest-neighbor interchange (NNI)



## How do you find the optimal tree?

Method	Result	Time	Typical k
<b>Exhaustive search</b>	Optimal solution	$T(k)$	12
<b>Branch and bound</b>	Optimal solution	$\leq T(k)$	18
<b>Heuristic search</b>	Suboptimal solution	<i>You choose</i>	<i>You choose</i>

## Finding the optimal tree

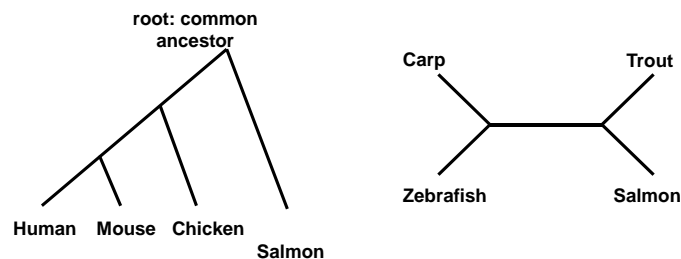
Given  $k$  taxa,

- Consider all trees with  $k$  leaves
- Score each tree with respect to chosen evolutionary model.
- Select highest scoring tree(s)

Criteria for evaluating which tree best fits the data:

- Maximum parsimony (character data)
- Minimum evolution (distance data)
- Maximum Likelihood (character data)

## Rooted vs unrooted trees:



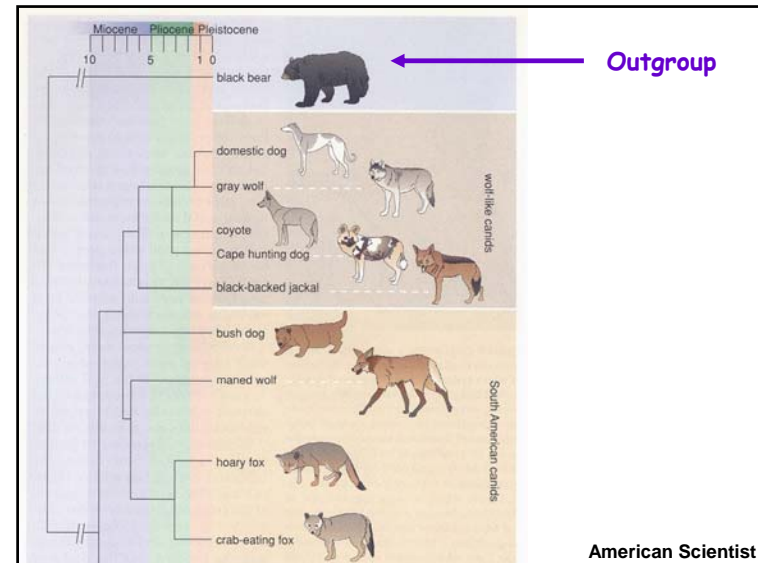
*Unrooted trees give no information about the order of speciation events*

## Unrooted vs. Rooted Trees

- An **unrooted** tree gives information about the relationships between taxa.
- A **rooted** gene tree gives information about the order of events.
- Most tree reconstruction programs output unrooted trees.

## How to root an unrooted tree

- If the mutation rate is constant in all lineages, the distance from root to leaf is the same for all leaves.
  - We can obtain a rooted tree algorithmically.
  - This is **midpoint rooting**.
- Otherwise, use an **outgroup**, a taxon that is distantly related to all other leaf taxa.



## Finding the optimal tree

Given  $k$  taxa,

- Consider all trees with  $k$  leaves
- Score each tree with respect to chosen evolutionary model.
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Criteria for evaluating which tree best fits the data:

- Maximum parsimony (character data)
- Minimum evolution (distance data)
- Maximum Likelihood (character data)

## Multiple Sequence Alignment as Character Data

Each column (or site) is one character.

```

~ ~ ~ ~ A L T E K Q E A L L K Q S W E V L K Q N I P A H S R L F A L I I E A A ...
~ ~ ~ ~ M A L T E K Q E A L L K Q S W E V L K Q N I P A H S R L F A L I I E A A ...
~ ~ ~ ~ M A L T E R Q E A L L K Q S W E V L K Q N I P G H S R L F A L I I E A A ...
~ ~ ~ ~ ~ ~ ~ ~ ~ ~ E A L L K Q S W E V L K Q N I P G H S C L F A L I I E A A ...
    
```

	C1	C2	C3	C4
Bees	A	H	S	R
Moths	A	H	S	R
Ants	G	H	S	R
Centipedes	G	H	S	C

## Multiple Sequence Alignment as Distance Data

Human ~~~~ALTEKQEALLKQSWEVLKQNI PAHSLRRLFALIEAA...  
 Rabbit ~~~MALTEKQEALLKQSWEVLKQNI PAHSLRRLFALIEAA...  
 Pig ~~~MALTERQEALLKQSWEVLKQNI PGHSLRRLFALIEAA...  
 Chicken ~~~~~EALLKQSWEVLKQNI PGHSLCLFALIEAA...

	Human	Rabbit	Pig	Chicken
Human	0	3	7	9
Rabbit		0	6	8
Pig			0	6
Chicken				0

### Assumptions:

- Selection dominates
- Mutations are rare
- No multiple substitutions

### Parsimony:

Character data  
 Find the tree that requires the fewest changes to explain the data

### Assumptions:

- Neutral mutation dominates
- Multiple substitutions occur

### Minimum Evolution:

Distance data  
 Find the tree that best fits the pairwise distances between taxa

### Maximum Likelihood:

Character data  
 Find the most likely tree

### Assumptions:

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### Parsimony:

Character data  
 Find the tree that requires the fewest changes to explain the data

### Assumptions:

- Neutral mutation dominates
- Multiple substitutions occur

### Minimum Evolution:

Distance data  
 Find the tree that best fits the pairwise distances between taxa

### Maximum Likelihood:

Character data  
 Find the most likely tree

## Distance-based methods

- How to obtain a distance matrix
- Correcting for multiple substitutions
- Fitting distances to a tree
  - Conditions for obtaining an exact fit
    - Ultrametric distances
    - Additive distances
  - Minimum Evolution: finding the tree with the best fit
  - Greedy algorithms
    - UPGMA
    - NeighborJoining

## How distance matrices are obtained

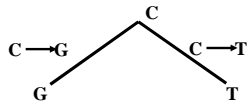
Given sequences from  $k$  taxa

- Construct a multiple sequence alignment
- Determine pairwise distance from each pair of taxa *using the MSA*
- Correct for multiple substitutions

## Multiple Sequence Alignment

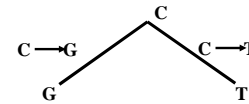
~~~~~ALTEKQEALLKQSWEVLKQNI PAHSLRLFALIT EAA...

## Substitution patterns

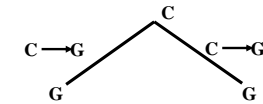


Coincidental substitution:

## Substitution patterns



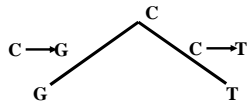
Coincidental substitution:  
- 2 changes, 1 difference



Parallel substitution:

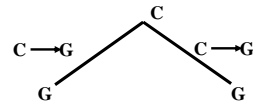
...G...  
...T...

## Substitution patterns



Coincidental substitution:  
- 2 changes, 1 difference

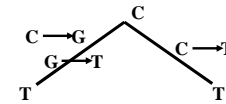
...G...  
...T...



Parallel substitution:  
- 2 changes, no difference

...G...  
...G...

## Substitution patterns



Convergent substitution:

## Substitution patterns



Convergent substitution:  
- 3 changes, no difference

...T...  
...T...

Back substitution:

## Substitution patterns



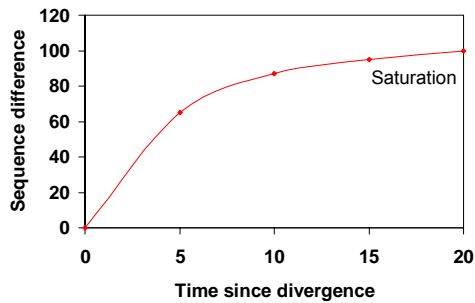
Convergent substitution:  
- 3 changes, no difference

...T...  
...T...

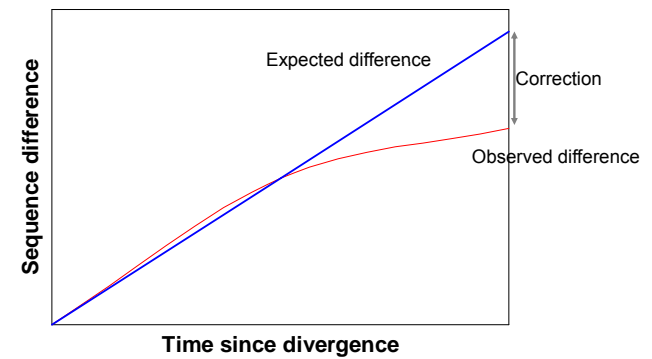
Back substitution:  
- 2 changes, no difference

...C...  
...C...

## Multiple substitutions

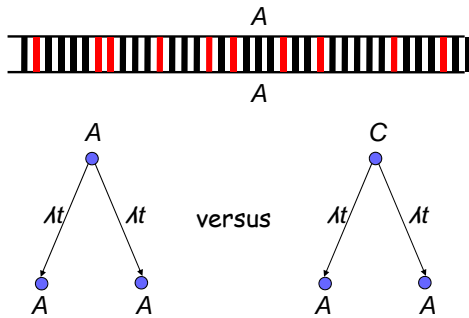


## Correcting for multiple substitutions



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Given  $m$  mismatches in a PW alignment of length  $n$ , estimate the actual number of substitutions



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Given  $m$  mismatches in a PW alignment of length  $n$ , estimate the actual number of substitutions

Note that:

$p' = m/n$  is an estimator for the underlying probability of a mismatch,  $p = P(\text{mismatch})$

The number of substitutions is  $2\lambda t$

Strategy

Propose a Markov model of substitution

Derive  $p = f(\lambda t)$

$\lambda t = f^{-1}(p)$

$E[\text{subs/site}] = 2 f^{-1}(p)$

