15-462 Computer Graphics I Lecture 17

Spatial Data Structures

Hierarchical Bounding Volumes

Regular Grids

Octrees

BSP Trees

Constructive Solid Geometry (CSG)

[Angel 8.9]

March 28, 2002
Frank Pfenning
Carnegie Mellon University

http://www.cs.cmu.edu/~fp/courses/graphics/

Ray Tracing Acceleration

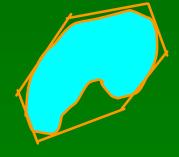
- Faster intersections
 - Faster ray-object intersections
 - Object bounding volume
 - Efficient intersectors
 - Fewer ray-object intersections
 - Hierarchical bounding volumes (boxes, spheres)
 - Spatial data structures
 - Directional techniques
- Fewer rays
 - Adaptive tree-depth control
 - Stochastic sampling
- Generalized rays (beams, cones)

Spatial Data Structures

- Data structures to store geometric information
- Sample applications
 - Collision detection
 - Location queries
 - Chemical simulations
 - Rendering
- Spatial data structures for ray tracing
 - Object-centric data structures (bounding volumes)
 - Space subdivision (grids, octrees, BSP trees)
 - Speed-up of 10x, 100x, or more

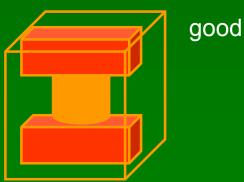
Bounding Volumes

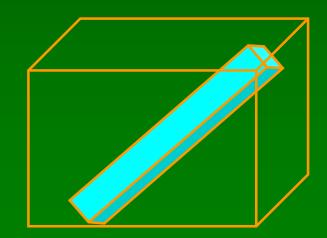
- Wrap complex objects in simple ones
- Does ray intersect bounding box?
 - No: does not intersect enclosed objects
 - Yes: calculate intersection with enclosed objects
- Common types
 - Boxes, axis-aligned
 - Boxes, oriented
 - Spheres
 - Finite intersections or unions of above



Selection of Bounding Volumes

- Effectiveness depends on:
 - Probability that ray hits bounding volume, but not enclosed objects (tight fit is better)
 - Expense to calculate intersections with bounding volume and enclosed objects
- Amortize calculation of bounding volumes
- Use heuristics





bad

Hierarchical Bounding Volumes

- With simple bounding volumes, ray casting still has requires O(n) intersection tests
- Idea use tree data structure
 - Larger bounding volumes contain smaller ones etc.
 - Sometimes naturally available (e.g. human figure)
 - Sometimes difficult to compute
- Often reduces complexity to O(log(n))

Ray Intersection Algorithm

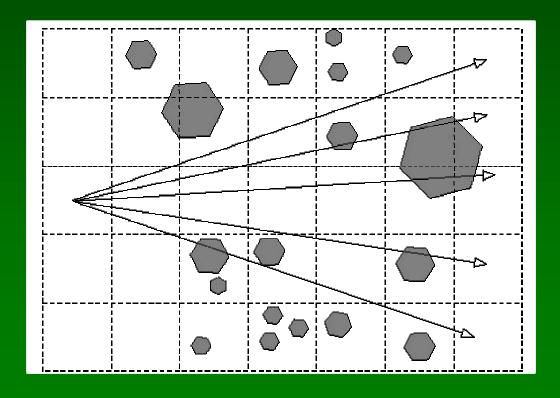
- Recursively descend tree
- If ray misses bounding volume, no intersection
- If ray intersects bounding volume, recurse with enclosed volumes and objects
- Maintain near and far bounds to prune further
- Overall effectiveness depends on model and constructed hierarchy

Spatial Subdivision

- Bounding volumes enclose objects, recursively
- Alternatively, divide space
- For each segment of space keep list of intersecting surfaces or objects
- Basic techniques
 - Regular grids
 - Octrees (axis-aligned, non-uniform partition)
 - BSP trees (recursive Binary Space Partition, planes)

Grids

- 3D array of cells (voxels) that tile space
- Each cell points to all intersecting surfaces
- Intersection alg steps from cell to cell



Caching Intersection points

- Objects can span multiple cells
- For A need to test intersection only once
- For B need to cache intersection and check next cell for closer one

• If not, C could be missed (yellow ray)

Assessment of Grids

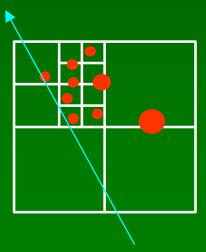
- Poor choice when world is non-homogeneous
- Size of grid
 - Too small: too many surfaces per cell
 - Too large: too many empty cells to traverse
 - Can use alg like Bresenham's for efficient traversal
- Non-uniform spatial subdivision more flexible
 - Can adjust to objects that are present

Outline

- Hierarchical Bounding Volumes
- Regular Grids
- Octrees
- BSP Trees
- Constructive Solid Geometry (CSG)

Quadtrees

- Generalization of binary trees in 2D
 - Node (cell) is a square
 - Recursively split into 4 equal sub-squares
 - Stop subdivision based on number of objects
- Ray intersection has to traverse quadtree
- More difficult to step to next cell



Octrees

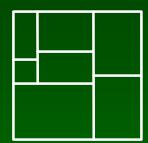
- Generalization of quadtree in 3D
- Each cell may be split into 8 equal sub-cells
- Internal nodes store pointers to children
- Leaf nodes store list of surfaces
- Adapts well to non-homogeneous scenes

Assessment for Ray Tracing

- Grids
 - Easy to implement
 - Require a lot of memory
 - Poor results for non-homogeneous scense
- Octrees
 - Better on most scenes (more adaptive)
- Alternative: nested grids
- Spatial subdivision expensive for animations
- Hierarchical bounding volumes
 - Natural for hierarchical objects
 - Better for dynamic scenes

Other Spatial Subdivision Techniques

- Relax rules for quadtrees and octrees
- k-dimensional tree (k-d tree)
 - Split at arbitrary interior point
 - Split one dimension at a time



- Binary space partitioning tree (BSP tree)
 - In 2 dimensions, split with any line
 - In k dims. split with k-1 dimensional hyperplane
 - Particularly useful for painter's algorithm
 - Can also be used for ray tracing [see handout]

Outline

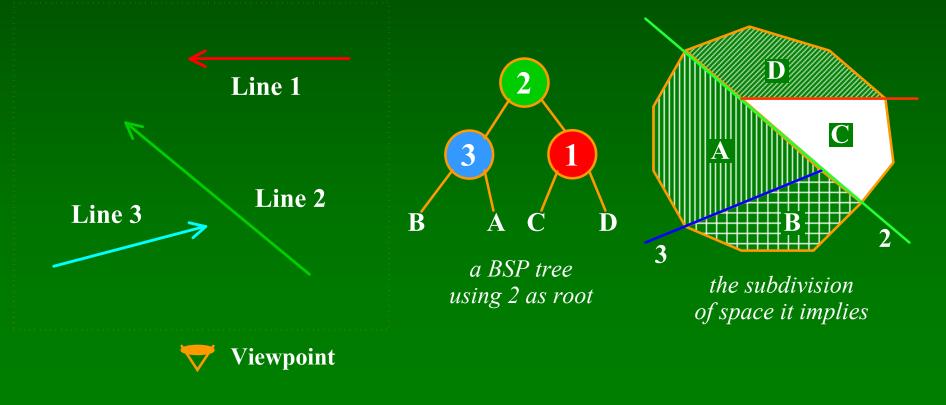
- Hierarchical Bounding Volumes
- Regular Grids
- Octrees
- BSP Trees
- Constructive Solid Geometry (CSG)

BSP Trees

- Split space with any line (2D) or plane (3D)
- Applications
 - Painters algorithm for hidden surface removal
 - Ray casting
- Inherent spatial ordering given viewpoint
 - Left subtree: in front, right subtree: behind
- Problem: finding good space partitions
 - Proper ordering for
 - Balance tree
- For details, see http://reality.sgi.com/bspfaq/

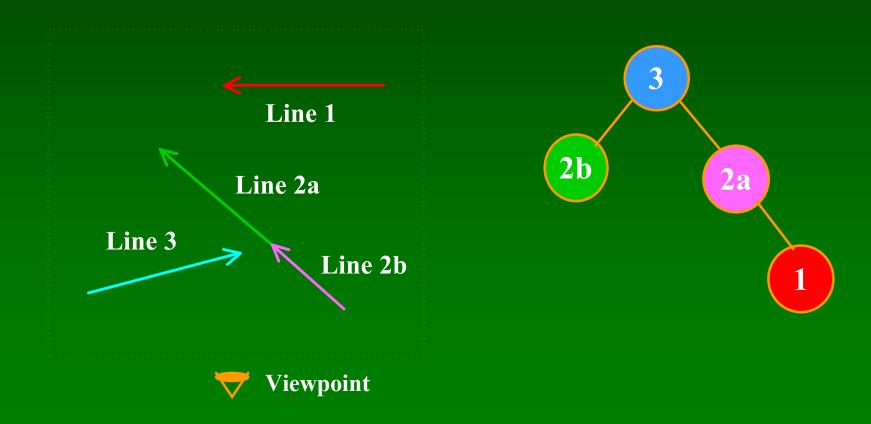
Building a BSP Tree

- Use hidden surface removal as intuition
- Using line 1 or line 2 as root is easy



Splitting of surfaces

Using line 3 as root requires splitting



Building a Good Tree

- Naive partitioning of n polygons yields O(n³) polygons (in 3D)
- Algorithms with O(n²) increase exist
 - Try all, use polygon with fewest splits
 - Do not need to split exactly along polygon planes
- Should balance tree
 - More splits allow easier balancing
 - Rebalancing?

Painter's Algorithm with BSP Trees

- Building the tree
 - May need to split some polygons
 - Slow, but done only once
- Traverse back-to-front or front-to-back
 - Order is viewer-direction dependent
 - What is front and what is back of each line changes
 - Determine order on the fly

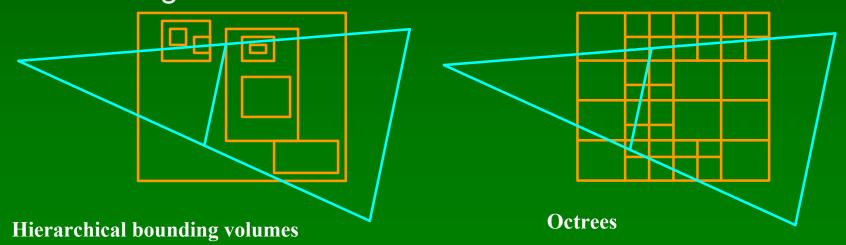
Details of Painter's Algorithm

- Each face has form Ax + By + Cz + D
- Plug in coordinates and determine
 - Positive: front side
 - Zero: on plane
 - Negative: back side
- Back-to-front: inorder traversal, farther child first
- Front-to-back: inorder traversal, near child first
- Do backface culling with same sign test
- Clip against visible portion of space (portals)

[Guest Lecture: John Ketchpaw]

Clipping With Spatial Data Structures

- Accelerate clipping
 - Goal: accept or rejects whole sets of objects
 - Can use an spatial data structures
- Scene should be mostly fixed
 - Terrain fly-through
 - Gaming



Data Structure Demos

- BSP Tree construction http://symbolcraft.com/pjl/graphics/bsp/
- KD Tree construction http://www.rolemaker.dk/nonRoleMaker/uni/algogem/kdtree.htm

Real-Time and Interactive Ray Tracing

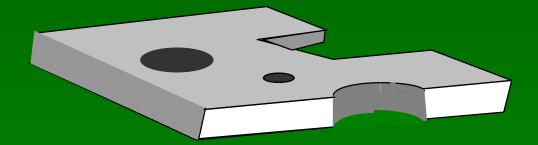
- Interactive ray tracing via space subdivision http://www.cs.utah.edu/~reinhard/egwr/
- Interactive ray tracing with good hardware http://www.cs.utah.edu/vissim/projects/raytracing/

Outline

- Hierarchical Bounding Volumes
- Regular Grids
- Octrees
- BSP Trees
- Constructive Solid Geometry (CSG)

Constructive Solid Geometry (CSG)

- Generate complex shapes with simple building blocks (boxes, spheres, cylinders, cones, ...)
- Particularly applicable for machined objects
- Efficient with ray tracing



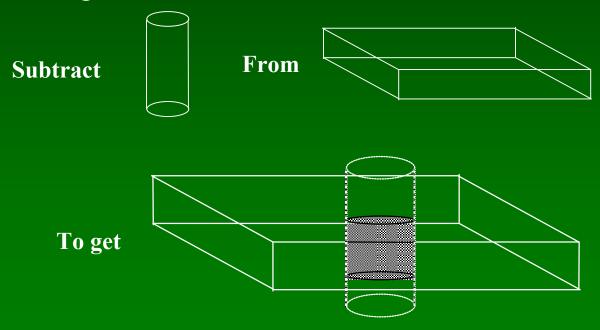
Example: A CSG Train



Brian Wyvill et al., U. of Calgary

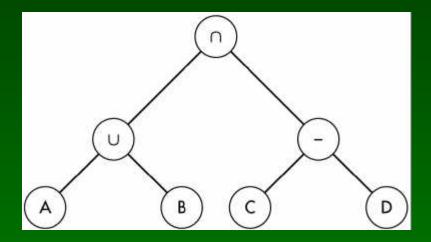
Boolean Operations

- Intersection and union
- Subtraction
 - Example: drilling a hole



CSG Trees

Set operations yield tree-based representation



- Use these trees for ray/objects intersections
- Think about how!

Implicit Functions for Booleans

- Solid as implicit function, F(x,y,z)
 - -F(x, y, z) < 0 interior
 - F(x, y, z) = 0 surface
 - F(x, y, z) > 0 exterior
- For CSG, use $F(x, y, z) \in \{-1, 0, 1\}$
- $F_{A \cap B}(p) = \max(F_A(p), F_B(p))$
- $F_{A \cup B}(p) = \min(F_A(p), F_B(p))$
- $F_{A-B}(p) = max(F_A(p), -F_B(p))$

Summary

- Hierarchical Bounding Volumes
- Regular Grids
- Octrees
- BSP Trees
- Constructive Solid Geometry (CSG)

Preview

- Radiosity
- Image Processing
- Assignment 6 due today
- Assignment 7 (ray tracing) out late today